# Synthesis, stability and structure of the complex of bismuth(III) with the nitrogen-donor macrocycle $\mathbf{1 , 4 , 7 , 1 0 \text { -tetraazacyclododecane. The }}$ role of the lone pair on bismuth(III) and lead(II) in determining co-ordination geometry 

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#### Abstract

The complex $\left[\mathrm{Bi}(\right.$ cyclen $\left.)\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{ClO}_{4}\right)_{3}\right]$ (cyclen = 1,4,7,10-tetraazacyclododecane) has been synthesized and its crystal structure determined. The Bi has square-antiprismatic co-ordination to the four nitrogens of cyclen (mean $\mathrm{Bi}-\mathrm{N} 2.39 \AA$ ) with the upper square being provided by one oxygen from each of the three perchlorates and a water molecule (mean $\mathrm{Bi}-\mathrm{O} 2.77 \AA$ ). The formation constant $\left(\log \mathrm{K}_{1}\right)$ of $\mathrm{Bi}{ }^{\prime \prime \prime}$ with cyclen has been determined as 23.45 at $\mathrm{I}=0.5 \mathrm{~mol} \mathrm{dm}{ }^{-3}$ and $25^{\circ} \mathrm{C}$ by differential pulse polarography in an out-of-cell technique, where equilibration was slow and required 6 months. This is a high $\log K_{1}$ value for a complex with cyclen, in accord with predictions made of the high affinity that $\mathrm{Bi}^{\prime \prime \prime}$ would have for polyamines on the basis of a model of acid-base interactions in aqueous solution. The structures of some complexes of $\mathrm{Bi}^{1 / 1}$ and the isoelectronic $\mathrm{Pb}^{\prime \prime}$ were analysed in terms of the effect that the lone pair of electrons has on the $M-L$ bond length ( $M=B i$ or $P b, L=$ ligand donor atom). A relationship was found between the $M-L$ bond length and the distance of $L$ from the lone pair as quantified by the I.p. $-M-L$ (I.p. = lone pair) angle, with $M-L$ decreasing as I.p. $-M-L$ increases. This observation is rationalized in terms of an analogy with the linear co-ordination geometry found in many complexes of $\mathrm{Hg}^{\prime \prime}$, where the lonepair on $\mathrm{Bi}^{\text {III }}$ or $\mathrm{Pb}{ }^{\text {II }}$ occupies oneof thetwo co-ordination sites in theanalogouslinear two-co-ordinate mercury(II) complex.


The chemistry of heavy post-transition elements such as Ga , $\mathrm{In}, \mathrm{TI}, \mathrm{Bi}$ and Pb has been somewhat neglected. Standard texts ${ }^{1-5}$ devote few pages to them as compared to the transition elements, for example. However, recent developments have highlighted the need for a deeper examination of this chemistry. Gallium and indium, as the ${ }^{57} \mathrm{Ga}$ and ${ }^{111} \mathrm{n}$ isotopes, are important ${ }^{6}$ in body-imaging techniques in medicine. The chemistry of lead is of interest in relation to its toxicity and effects on intelligence in human populations. ${ }^{7}$ Bismuth has become of increasing interest, as its ${ }^{212} \mathrm{Bi}$ isotope in potential cancer therapies, ${ }^{8}$ and the use of complexes such as the subsalicylate in treating gastric and duodenal ulcers. ${ }^{9}$ The increasing interest in bismuth has recently led to papers on its chemistry with chelating ligands. ${ }^{10-16}$ Polarographic studies ${ }^{10,11}$ haveshown that the bismuth(III) ion has considerable affinity for nitrogen-donor ligands. Thus, $\log \mathrm{K}_{1}$ for $\mathrm{Bi}^{\prime \prime \prime}$ with ${ }^{10,11}$ some polyamine ligands can be compared with values reported ${ }^{17}$ for the same ligands with $\mathrm{Cu}^{11}$ and $\mathrm{Hg}^{11}$, which are regarded as having a high affinity for ligands with neutral nitrogen donors (Table 1). Constants for the isoelectronic Pb " are also included.

What was pleasing ${ }^{10,11}$ about the observed high affinity of Bi'II for nitrogen-donor ligands was that it was predicted ${ }^{18}$ several years before any attempt was made ${ }^{10,11}$ to demonstrate it. In 1978 one of the present authors co-authored a paper ${ }^{18}$ in which an equation was presented that allowed for prediction of $\log K_{1}$ values for metal ions with unidentate ligands, similar to that proposed by Drago and Wayland ${ }^{19}$ for predicting enthalpies of Lewis acid-base interactions in solvents of low relative permittivity. The estimate of $\log \mathrm{K}_{1}\left(\mathrm{NH}_{3}\right)$ for $\mathrm{Bi}^{\prime \prime \prime}$ of 5.0 suggested high affinity for polydentate ligands. The method of estimation of $\log \mathrm{K}_{1}$ has been discussed ${ }^{10,11,18,20}$ in some detail, so that here we point out only that rearrangement of the

Table 1 Formation constants of $\mathrm{Bi}($ III $)$ and other metal ions with nitrogen donor ligands

|  | $\log K_{1}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| M etal ion | $\mathrm{NH}_{3}$ | ampy | dien | trien | [15]aneN 4 |
| Bi'I' | (5.0) ${ }^{\text {a }}$ | 9.4 | 17.5 | 21.9 | 23.5 |
| Cu' | 4.1 | 9.5 | 16.0 | 20.1 | 24.4 |
| H $\mathrm{g}^{\prime \prime}$ | 8.8 | (10.0) ${ }^{\text {b }}$ | 21.8 | 24.8 | 23.7 |
| Pb ${ }^{\prime \prime}$ | 1.6 | 3.95 | 7.5 | 10.4 | 10.5 |

ampy $=2-($ A minomethyl $)$ pyridine; dien $=$ diethylenetriamine; trien $=$ triethylenetetramine; [15]aneN ${ }_{4}=1,4,8,12$-tetraazacyclopentadecane. ${ }^{\text {a }}$ E stimated ${ }^{10,11,18}$ as discussed below. ${ }^{\text {b }}$ E stimated as half $\log \beta_{2}$. Formation constants from refs. 10,11 and 17.

Drago-Wayland equation, ${ }^{19}$ adapted for use in aqueous solution, ${ }^{18}$ yields equation (1).

$$
\begin{equation*}
\log K_{1}\left(\mathrm{NH}_{3}\right)=0.881 \log \mathrm{~K}_{1}\left(\mathrm{OH}^{-}\right)-1.08 \log \mathrm{~K}_{1}\left(\mathrm{~F}^{-}\right) \tag{1}
\end{equation*}
$$

Equation (1) yields $\log \mathrm{K}_{1}\left(\mathrm{NH}_{3}\right)$ from the known values of $\log \mathrm{K}_{1}$ for the hydroxide and fluoride complexes to within about $0.4 \log$ units for metal ions for which $\log \mathrm{K}_{1}\left(\mathrm{NH}_{3}\right)$ can be determined experimentally. The predicted value of $\log \mathrm{K}_{1}\left(\mathrm{NH}_{3}\right)$ for Bill' of 5.0 suggests that the ammonia complexes of Bill will not exist in aqueous solution, because of hydrolysis according to equation (2). With $\log \mathrm{K}_{1}\left(\mathrm{OH}^{-}\right)$for $\mathrm{Bi}^{\prime \prime \prime}$ of $12.36, \mathrm{pK}_{\mathrm{w}}$ of

$$
\left[\mathrm{Bi}\left(\mathrm{NH}_{3}\right)\right]^{3+}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons[\mathrm{Bi}(\mathrm{OH})]^{2+}(\mathrm{aq})+\mathrm{NH}_{4}^{+}(\mathrm{aq})
$$

14.0, and with ${ }^{17}$ the $\mathrm{pK}_{\mathrm{a}}$ for $\mathrm{NH}_{4}{ }^{+}$of 9.22 , one calculates that reaction (2) will proceed to the right with a quotient of $10^{2.58}$. M any metal ions, such as $\mathrm{Fe}^{\text {III, }} \mathrm{Pu}^{\mathrm{IV}}$ and $\mathrm{Bi}^{\mathrm{III}}$, which are


$L^{3}$

tprp

$L^{2}$

$L^{4}$

$L^{6}$

$\mathrm{H}_{4}$ edta

$\mathrm{H}_{3}$ nta
traditionally regarded ${ }^{1-5}$ as having low affinity for amines, are predicted to have high $\log \mathrm{K}_{1}$ values with ammonia, but these complexes do not exist in solution because of the high affinity these metal ions have for $\mathrm{OH}^{-}$. H owever, the chelate effect can stabilize ${ }^{21}$ the complexes of these metal ions with polyamines, so that these are less prone to hydrolysis in aqueous solution. Thus it has been possible to measure the formation constants of $\mathrm{Bi}^{\text {III }}$ with polyamine ligands, both open-chain and macrocyclic.

In this paper the chemistry of $\mathrm{Bi}^{\prime \prime \prime}$ with nitrogen-donor macrocycles is investigated further. The synthesis and structure of a complex of $\mathrm{Bi}^{\text {l"I }}$ with the pendant-donor macrocycle $\mathrm{L}^{1}$ has already been reported. ${ }^{12}$ We report here the synthesis of the first example of a complex of $\mathrm{Bi}^{i 11}$ with a non-pendant-donor tetraazamacrocycle, $\left[\mathrm{Bi}(\right.$ cyclen $)\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{ClO}_{4}\right)_{3}$ ], a crystallographic study of its structure, and a polarographic determination of the stability of the complex of $\mathrm{Bi}^{1 \text { II }}$ with cyclen in aqueous solution. Polarography has been shown ${ }^{10,11}$ to be particularly suited to the study of complexes of hydrolysis-prone metal ions such as $\mathrm{Bi} \mathrm{i}^{\prime \prime}$.
The bismuth(III) and lead(II) ions have lone pairs of electrons, which can be stereochemically active, ${ }^{22}$ and exert a considerable effect on the structures of their complexes. The stereochemically active lone pair can also ${ }^{23}$ affect the thermodynamic stability of the complexes of these ions. A $n$ attempt is made here to rationalize further the thermodynamic and structural effects of the lone pair on these ions.

## Experimental

## M aterials

The compound cyclen was synthesized according to the method of Richman and Atkins. ${ }^{24}$ The complex $\left[\mathrm{Bi}(\right.$ cyclen $)\left(\mathrm{H}_{2} \mathrm{O}\right)$ $\left(\mathrm{ClO}_{4}\right)_{3}$ ] was synthesized by dissolving $\mathrm{Bi}_{2} \mathrm{O}_{3}$ in $70 \% \mathrm{HClO}_{4}$, together with 1 equivalent of cyclen. The pH was adjusted to approximately 1.0 by addition of $\mathrm{Na}_{2} \mathrm{CO}_{3}$. On standing, small colourless crystals were deposited, which were filtered off (Found: C, $30.0 ; \mathrm{H}, 3.15 ; \mathrm{N}, 8.15$. Calc. for $\mathrm{C}_{8} \mathrm{H}_{22} \mathrm{BiCl}_{3} \mathrm{~N}_{4} \mathrm{O}_{13}$ : C, 29.95; H, 3.2; N, 8.05\%). CAUTION: Organic perchlorates may be explosive.

All reagents used for polarography were of analytical grade ( M erck). Pure water was obtained by passing deionized water through a Milli-Q water-purification system. A $5.123 \times 10^{-3}$ $\mathrm{mol} \mathrm{dm}{ }^{-3}$ stock solution of bismuth(iII) nitrate was prepared in $0.5 \mathrm{~mol} \mathrm{dm}^{-3} \mathrm{HNO}_{3}$. All experiments were carried out at an ionic strength of $0.5 \mathrm{~mol} \mathrm{dm}^{-3}$.

## X-R ay crystallography

A colourless crystal of $\left[\mathrm{Bi}(\right.$ cyclen $\left.)\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{ClO}_{4}\right)_{3}\right] 1$ was mounted on a glass fibre at room temperature. Preliminary examination and data collection was performed on a Rigaku AFC5 (oriented graphite monochromator; M o-K $\alpha$ radiation) at 293(2) K. Cell parameters were calculated from least-squares fitting of 25 high-angle reflections ( $2<\theta<15^{\circ}$ ). $\omega$ Scans for several intense reflections indicated acceptable crystal quality. D ata were collected for $\theta 2.29-25.05^{\circ}$ at $163(2) \mathrm{K}$. The scan width was $1.54+0.3 \tan \theta$ in $\omega$ with a variablescan rateof $16^{\circ} \mathrm{min}^{-1}$. Weak reflections were rescanned (maximum of two rescans) and the counts for each scan were accumulated. Three standards, collected every 150 reflections, showed no significant trends. Background measurement was by the stationary crystal-stationary counter technique at the beginning and end of each scan for half the total scan time. L orentz-polarization corrections were applied to 1842 reflections. These unique observed reflections were used in further calculations. A n empirical absorption correction was applied. ${ }^{25}$ The structure was solved by direct methods. ${ }^{26} \mathrm{~F}$ ull-matrix least-squares anisotropic refinement for all non-hydrogen atoms yielded $w R=0.1762$ and $R=0.0614$ at convergence ${ }^{27} \mathrm{~N}$ eutral atom scattering factors and anomalous scattering factors were taken from ref. 28. The structure analysis showed disorder of the cyclen ring, over a crystallographic mirror plane passing through $\mathrm{Bi}, \mathrm{O}(1)$ and $\mathrm{CI}(1)$. The two disordered cyclen moieties, corresponding to RRRR and SSSS enantiomers, were given $50 \%$ site occupancy factors. R igid bond restraints were applied to all carbon and nitrogen atoms of the macrocyclic ring. ${ }^{29}$ The nitrogens co-ordinated to the bismuth were common to both disordered moieties. The hydrogen atoms (only those of water were included) were found in a Fourierdifference map and fixed to ride on the water oxygen position
( $U_{\text {iso }}=0.08$ ). Crystal data and details of structure refinement and selected bond lengths and angles are given in Tables 2 and 3.

A tomic co-ordinates, thermal parameters, and bond lengths and angles have been deposited at the Cambridge Crystallographic Data Centre (CCDC). See Instructions for Authors, J. Chem. Soc., D alton Trans., 1997, Issue 1. A ny requests to the CCDC for this material should quote the full literature citation and the reference number 186/322.

## Polarography

Differential pulse (DP) polarograms were recorded on a M etrohm 626 POLARECORD instrument fitted with a 626 VA stand. A multimode electrode ( M etrohm) was employed as working electrode, and used in the dropping mercury electrode mode with a drop time of 2 s . A Ag-AgCl electrode was used as the reference, and a platinum electrode as the auxiliary. A computer-generated DP waveform was used with the following characteristics: pulse height, 50 mV ; step height, 4 mV ; pulse width, 200 ms ; integration time, 60 ms . High-purity nitrogen was used for deaeration of the cell. ThepH of the solutions was recorded to $\pm 0.002 \mathrm{pH}$ unit on a PHI 72 pH meter and No . 39536 glass electrode (Beckman). The temperature of the cell was controlled to $25.0 \pm 0.1^{\circ} \mathrm{C}$.
The equilibration of the Bi"I' cyclen system in aqueous solution is very slow, so that an 'out-of-cell' technique was used for the stability constant study. A series of sample solutions was measured in glass vials by metering out $10 \mathrm{~cm}^{3}$ of $0.5 \mathrm{~mol} \mathrm{dm}^{-3}$ $\mathrm{HNO}_{3}$ and $0.5 \mathrm{~cm}^{3}$ of $5.123 \times 10^{-3} \mathrm{~mol} \mathrm{dm}{ }^{-3} \mathrm{Bi}\left(\mathrm{NO}_{3}\right)_{3}$ stock solution and adding solid cyclen ( 22.1 mg ). The initial concentration of $\mathrm{Bi}^{3+}$ was $2.44 \times 10^{-4} \mathrm{~mol} \mathrm{dm}^{-3}$, and the cyclen to metal ratio was 50.8: 1. The pH of the solutions was adjusted by the addition of $0.5 \mathrm{~mol} \mathrm{dm}^{-3} \mathrm{NaOH}$ and varied from sample to sample over the range $\mathrm{pH} 0.3-1.0$. Polarograms were run from time to time of these solutions kept at $25.0 \pm 1.0^{\circ} \mathrm{C}$, and after 7 months it was apparent that equilibrium had been attained since the polarograms recorded showed no change from those recorded after 6 months.

In a typical run, the first polarogram was recorded for a solution containing $0.5 \mathrm{~mol} \mathrm{dm}{ }^{-3} \mathrm{HNO}_{3}$ to check for impurities. Then one of the Bi -cyclen solutions (ca. $10 \mathrm{~cm}^{3}$ ) was transferred to the polarographic cell and deaerated. Two D P polarograms were recorded in the potential range 0.2 to -0.7 V . The solution was then transferred back to its vial, and the polarographic cell was cleaned with $0.5 \mathrm{~mol} \mathrm{dm}{ }^{-3} \mathrm{HNO}_{3}$ prior to examination of the next solution. The final solution for which a polarogram was recorded was a standard solution of $\mathrm{Bi}^{3+}$ $\left(2.44 \times 10^{-4} \mathrm{~mol} \mathrm{dm}^{-3}\right)$ in $0.5 \mathrm{~mol} \mathrm{dm}^{-3} \mathrm{HNO}_{3}$. This was done in order to provide a calibration for the concentration of free $\mathrm{Bi}^{3+}$ in the Bi -cyclen solutions. Polarograms were recorded on the samples once a month.

## C alculation of formation constants

A computer program M LSPEC, ${ }^{30}$ written for the IBM personal computer, which allowed for correction for the hydrolysis of $\mathrm{Bi}^{3+}$ to give species such as $[\mathrm{Bi}(\mathrm{OH})]^{2+}$ or $\left[\mathrm{Bi}_{6}(\mathrm{OH})_{12}\right]^{6+}$ using reported ${ }^{17}$ formation constants, was used to analyse the $\mathrm{Bi}^{111}$ cyclen solutions. It essentially solves the appropriate massbalance equations incorporating the estimated formation constants for the complexes thought to be present in solution, equation (3), where $x$ is the number of metal atoms $M$ in the

$$
\begin{equation*}
M_{T}=\Sigma M_{x} L_{y} H_{z} \tag{3}
\end{equation*}
$$

solution species, $y$ the number of ligands $L$ present, and $z$ the number of protons H (a hydroxide is a negative proton i.e. $\mathrm{z}=-1$ ). For hydroxo complexes such as $[\mathrm{Bi}(\mathrm{OH})]^{2+}(\mathrm{x}=1$, $y=0, z=-1$ ) the known ${ }^{17}$ formation constants were kept fixed in solving the mass-balance equation. The predicted species distribution with trial values of the unknown formation constants


Fig. 1 Structure of $\left[\mathrm{Bi}(\right.$ cyclen $\left.)\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{ClO}_{4}\right)_{3}\right]$, showing the numbering scheme. Only one of the disordered pair of cyclen ligands is shown for clarity. The complex lies over a crystallographic mirror plane containing $\mathrm{O}(1), \mathrm{Bi}(1)$ and $\mathrm{Cl}(1)$. A toms indicated with an 'a' only e.g. $O$ (7a) are related to the corresponding atom $O(7)$ by reflection through the mirror plane, while those indicated with a dash e.g. $\mathrm{C}\left(2 a^{\prime}\right)$ are related by reflection to an atom $\mathrm{C}\left(2^{\prime}\right)$ of the other individual constituting the disordered pair (not shown). The water [0(1)] and perchlorates containing $\mathrm{Cl}(2)$ and $\mathrm{CI}(2 \mathrm{a})$ are common to both disordered moieties, but that containing $\mathrm{Cl}(1)$ has a second set of oxygens [ $\mathrm{O}(2 \mathrm{a})$ to $\mathrm{O}(5 \mathrm{a})$ ] present in the other disordered unit, related to 0 (2)-O(5) by reflection through the mirror plane. The thermal ellipsoids are at the 50\% probability level
and the relevant solution concentrations and pH were then compared with those indicated by the polarograms, and the formation constants adjusted to give as close a fit as possible. Peak currents rather than integrated peak currents were used as a measure of concentration. No evidence for adsorption effects or kinetic effects was found in the polarograms.

## Results and Discussion

## X-R ay crystallography

The structure of $\left[\mathrm{Bi}(\right.$ cyclen $\left.)\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{ClO}_{4}\right)_{3}\right] \mathbf{1}$ is seen in Fig .1 (see also Tables 2 and 3 ), where only one disordered moiety is shown. The co-ordination geometry of Bi in $\mathbf{1}$, and in its complex with $\mathrm{L}^{1}$ is shown in Fig. 2. A lso shown for comparison is the coordination geometry around the isoelectronic lead(II) ion in its complex with L ${ }^{123}$ Thestructure of 1 shows the similarity of the co-ordination geometry of $\mathrm{Bi}^{\prime \prime \prime}$ to that of $\mathrm{Pb}{ }^{\prime \prime}$. The difference in bond lengths $\mathrm{Bi}-\mathrm{N}$ (mean $=2.39 \AA$ ) and $\mathrm{Bi}-\mathrm{O}$ (mean $=$ $2.77 \AA$ ) compared to $\mathrm{Pb}-\mathrm{N} 2.64, \mathrm{~Pb}-\mathrm{O} 2.75 \AA$ reflects the smaller ionic radius ${ }^{31}$ of $\mathrm{Bi}^{\mathrm{I} \mathrm{\prime} \mathrm{\prime}}$. In 1, the co-ordination geometry is square antiprismatic, with the four nitrogens of the macrocycle forming one square, and the four oxygen donors another. In the $\mathrm{L}^{1}$ complexes of both $\mathrm{Bi}^{11 \mathrm{II}}$ and $\mathrm{Pb}^{11}$ the structure is distorted from square antiprismatic towards cubic, probably due to the shortness of the pendant alcohol groups preventing rotation of the oxygen donors into a regular squareantiprismatic structure
A conspicuous feature of the structures of the complexes of $\mathrm{Bi}^{1 I \prime}$ and $\mathrm{Pb}^{11}$ is the effect of the Ione pair of electrons on $\mathrm{L}-\mathrm{M}-\mathrm{L}$ bond angles and lengths. ${ }^{31}$ In an initial study of this problem ${ }^{23}$ the structure of $\left[\mathrm{PbL}^{1}\right]\left[\mathrm{NO}_{3}\right]_{2} \cdot \mathrm{Pr}{ }^{\mathrm{n}} \mathrm{OH}$ was determined. Although it was concluded ${ }^{23}$ that the $\mathrm{Pb}^{11}$ might in fact not have a stereochemically active lone pair, in light of the present work it seems clear that the lone pair in [ $\left.\mathrm{PbL}{ }^{1}\right]\left[\mathrm{NO}_{3}\right]_{2}$. $\mathrm{Pr}^{\mathrm{n} O H}$ is active. The structure showed the geometry around Pb " to possess features associated ${ }^{22,33,34}$ with a stereochemically active lone pair, namely, (1) a gap in the co-ordination where the


Fig. 2 Stereoviews of the co-ordination geometry around $\mathrm{Pb}^{\prime \prime}$ and $\mathrm{Bi}^{\prime \prime \prime}$. The geometry around $\mathrm{Bi}^{\prime \prime \prime}$ is shown (a) in $\left[\mathrm{Bi}(\mathrm{cyclen})\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{ClO}_{4}\right)_{3}\right]$, determined in this work, and (b) in $\left[\mathrm{BiL}^{1}\right]\left[\mathrm{ClO}_{4}\right]_{3} .^{12}$ The geometry around $\mathrm{Pb}^{11}$ is shown (c) in $\left[\mathrm{PbL}^{1}\right]\left[\mathrm{NO}_{3}\right]_{2} \cdot \mathrm{Pr}^{n} \mathrm{OH}$, ${ }^{31}$ and (d) in $\left[\mathrm{PbL}^{2}(\mathrm{SCN})_{2}\right]^{32}$ Oxygen atoms are shown as black circles, nitrogen as cross-hatched and sulfurs as larger open circles. The Pb and Bi atoms are shown as large shaded circles. The proposed positions of the lone pairs are indicated as very small circles at the end of broken lines. M etal-ligand bonds which are longer than expected from the sums of the ionic radii are indicated as broken lines. D rawings made with coordinates available in the original papers ${ }^{12,31,32}$

Table 2 Crystal data and structure refinement for $\left[\mathrm{Bi}(\right.$ cyclen $)\left(\mathrm{H}_{2} \mathrm{O}\right)$ $\left.\left(\mathrm{ClO}_{4}\right)_{3}\right]$

| Empirical formula | $\mathrm{C}_{8} \mathrm{H}_{22} \mathrm{BiCl}_{3} \mathrm{~N}_{4} \mathrm{O}_{13}$ |
| :---: | :---: |
| $\lambda / \AA$ 砍 | 0.71073 |
| Crystal system | Orthorhombic |
| Space group | P nma |
| a/Å | 17.784(4) |
| b/Å | 13.429(5) |
| c/Å | 8.390(2) |
| $U / \AA^{3}$ | 2003.7(10) |
| Z | 4 |
| $\mathrm{D}_{\mathrm{c}} / \mathrm{mg} \mathrm{m}^{-3}$ | 2.30 |
| $\mathrm{D}_{\mathrm{m}} / \mathrm{mg} \mathrm{m}^{-3}$ | 2.29 |
| $\mu / \mathrm{mm}^{-1}$ | 9.270 |
| F (000) | 1328 |
| Crystal size/mm | $0.44 \times 0.44 \times 0.38$ |
| Index ranges | $\begin{aligned} & 0 \leqslant h \leqslant 21,-16 \leqslant k \leqslant 0,-9 \leqslant \\ & \mid \leqslant 0 \end{aligned}$ |
| R eflections collected | 1842 |
| Independent reflections | $1842\left(\mathrm{R}_{\text {int }}=0.0000\right)$ |
| R efinement method | F ull-matrix least squares on $\mathrm{F}^{2}$ |
| D ata, restraints, parameters | 1806, 269, 190 |
| Goodness of fit on $\mathrm{F}^{2}$ | 1.050 |
| Final R 1, wR $2[1>2 \sigma(1)]$ | 0.0517, 0.1446 |
| (all data) | 0.0614, 0.1762 |
| L argest difference peak and hole/e $\AA^{-3}$ | 1.572, -1.616 |
| wR $2=\Sigma\left[\left(F_{0}{ }^{2}-F_{c}{ }^{2}\right)^{2}\right]^{\frac{1}{2}}\left(F_{0}{ }^{2}\right)^{2}$. where $a=0.1096$ and $b=13.727$ | $g, \quad w=1 /\left[\sigma\left(F_{o}{ }^{2}\right)+\left(a F_{o}{ }^{2}+b F_{o}{ }^{2}\right)\right]$ |

Ione pair is thought to be located and (2) shortening of the $\mathrm{Pb}-\mathrm{L}$ bonds on the side of the Pb " away from the proposed site of the lone pair. The structures in Fig. 3 all show this feature with short $\mathrm{Pb}-\mathrm{N}$ or $\mathrm{Bi}-\mathrm{N}$ and long $\mathrm{M}-\mathrm{O}$ bonds. In most cases, $\mathrm{M}-\mathrm{N}$ bonds are longer than $\mathrm{M}-\mathrm{O}$ bonds, which relates to the smaller size ${ }^{29}$ of oxygen than nitrogen. Bismuth(III) in its com-

Table 3 Selected bond lengths $(\AA)$ and angles $\left({ }^{\circ}\right)$ in $\left[\mathrm{Bi}(\right.$ cyclen $)\left(\mathrm{H}_{2} \mathrm{O}\right)$ $\left.\left(\mathrm{ClO}_{4}\right)_{3}\right]$

| $\mathrm{Bi}(1)-\mathrm{N}(1)$ | $2.375(10)$ | $\mathrm{Bi}(1)-\mathrm{N}(2)$ | $2.412(9)$ |
| :--- | :---: | :--- | ---: |
| $\mathrm{Bi}(1)-\mathrm{O}(4)$ | $2.81(2)$ | $\mathrm{Bi}(1)-\mathrm{O}(1)$ | $2.810(14)$ |
| $\mathrm{Bi}(1)-\mathrm{O}(7)$ | $2.690(10)$ |  |  |
| $\mathrm{N}(1)-\mathrm{Bi}(1)-\mathrm{N}\left(1^{\prime}\right)$ | $72.3(4)$ | $\mathrm{N}(1)-\mathrm{Bi}(1)-\mathrm{N}\left(2^{\prime}\right)$ | $113.3(4)$ |
| $\mathrm{N}(1)-\mathrm{Bi}(1)-\mathrm{N}(2)$ | $73.5(4)$ | $\mathrm{N}(2)-\mathrm{Bi}(1)-\mathrm{N}\left(2^{\prime}\right)$ | $70.4(5)$ |
| $\mathrm{N}(1)-\mathrm{Bi}(1)-\mathrm{O}(7)$ | $143.3(3)$ | $\mathrm{N}(1)-\mathrm{Bi}(1)-\mathrm{O}\left(7^{\prime}\right)$ | $77.4(4)$ |
| $\mathrm{N}(2)-\mathrm{Bi}(1)-\mathrm{O}\left(7^{\prime}\right)$ | $76.2(5)$ | $\mathrm{N}(2)-\mathrm{Bi}(1)-\mathrm{O}(7)$ | $139.3(3)$ |
| $\mathrm{O}(7)-\mathrm{Bi}(1)-\mathrm{O}\left(7^{\prime}\right)$ | $119.7(9)$ | $\mathrm{N}(1)-\mathrm{Bi}(1)-\mathrm{O}(4)$ | $154.4(6)$ |
| $\mathrm{N}(1)-\mathrm{Bi}(1)-\mathrm{O}(4)$ | $126.6(5)$ | $\mathrm{N}(2)-\mathrm{Bi}(1)-\mathrm{O}(4)$ | $65.6(6)$ |
| $\mathrm{N}(2)-\mathrm{Bi}(1)-\mathrm{O}(4)$ | $83.3(6)$ | $\mathrm{O}(7)-\mathrm{Bi}(1)-\mathrm{O}(4)$ | $62.6(6)$ |
| $\mathrm{O}(7)-\mathrm{Bi}(1)-\mathrm{O}(4)$ | $89.3(5)$ | $\mathrm{N}(1)-\mathrm{Bi}(1)-\mathrm{O}(1)$ | $72.2(4)$ |
| $\mathrm{N}(2)-\mathrm{Bi}(1)-\mathrm{O}(1)$ | $141.0(3)$ | $\mathrm{O}(7)-\mathrm{Bi}(1)-\mathrm{O}(1)$ | $79.3(3)$ |
| $\mathrm{O}(4)-\mathrm{Bi}(1)-\mathrm{O}(1)$ | $126.1(7)$ | $\mathrm{Cl}(1)-\mathrm{O}(4)-\mathrm{Bi}(1)$ | $132.3(13)$ |
| $\mathrm{C}\left(2^{\prime}\right)-\mathrm{N}(1)-\mathrm{Bi}(1)$ | $123.2(10)$ | $\mathrm{C}(2)-\mathrm{N}(1)-\mathrm{Bi}(1)$ | $103.5(10)$ |
| $\mathrm{C}(1)-\mathrm{N}(1)-\mathrm{Bi}(1)$ | $108.4(9)$ | $\mathrm{C}\left(1^{\prime}\right)-\mathrm{N}(1)-\mathrm{Bi}(1)$ | $115.4(10)$ |
| $\mathrm{C}\left(4^{\prime}\right)-\mathrm{N}(2)-\mathrm{Bi}(1)$ | $118.4(14)$ | $\mathrm{C}\left(3^{\prime}\right)-\mathrm{N}(2)-\mathrm{Bi}(1)$ | $108.6(11)$ |

plexes with cyclen in $\mathbf{1}$, and with $\mathrm{L}^{1}$, also shows $\mathrm{Bi}-\mathrm{N}$ bonds that are shorter than the $\mathrm{Bi}-\mathrm{O}$ bonds. What is of particular interest is the presence in the $\left[\mathrm{BiL}^{1}\right]\left[\mathrm{ClO}_{4}\right]_{3}$ and $\left[\mathrm{PbL}^{1}\right]\left[\mathrm{ClO}_{4}\right]_{2} \cdot \mathrm{Pr}{ }^{\mathrm{O} O H}$ complexes of very long $\mathrm{M}-\mathrm{O}$ contacts at the spot where the Ione pair is presumed to be. There is thus a $\mathrm{Bi}-\mathrm{O}$ contact at $3.34 \AA$ with an oxygen from a perchlorate, and the $\mathrm{Pb}^{\text {II }}$ is $3.50 \AA$ from the oxygen of the solvent PriOH molecule. The nature of this type of contact in these structures is not yet clear. There is no sign of similar contacts over the proposed sites of the lone pairs in 1 , or in the $\left[\mathrm{PbL}^{1}\right]\left[\mathrm{NO}_{3}\right]_{2} \cdot \mathrm{Pr}^{\mathrm{n}} \mathrm{OH}$ complex, ${ }^{31}$ with the nearest oxygens being over $4.5 \AA$ away. H owever, the structure of the $\left[\mathrm{PbL}^{1}\right]^{2+}$ cation is almost identical in the nitrate, where no contact with a donor atom is present over the site of the lone pair, and in the perchlorate, where such a contact is present.


Fig. 3 Relationship between the $\mathrm{Pb}-\mathrm{L}$ distance in some complexes of $\mathrm{Pb}^{\text {¹ }}$ and the I.p. $-\mathrm{Pb}-\mathrm{L}$ angle (I.p. = lone pair on $\mathrm{Pb}^{\text {II }}$ ). The structures from which bond length and angle data were taken were $\left[\mathrm{PbL}^{1}\right]^{2+}(\Delta)$, $\left[\mathrm{Pb}\left([9] \mathrm{aneN}_{3}\right)\left(\mathrm{N} \mathrm{O}_{3}\right)_{2}\right] \quad(\bigcirc), \quad\left[\mathrm{PbL}^{2}\right]^{2+} \quad(\mathrm{O}), \quad\left[\mathrm{Pb}\left([14] \mathrm{aneN}_{4}\right)\right]\left[\mathrm{N} \mathrm{O}_{3}\right]_{2}$ ([14]aneN ${ }_{4}=1,4,8,11$-tetraazacyclotetradecane) (©), [Pb(tprp)] ( $\diamond$ ), $\left[\mathrm{Pb}\left([16] a n e N_{4}\right)\right] \mathrm{Cl}_{2}(\square),\left[\mathrm{PbL}^{3}\right]^{2+}(\nabla),\left[\mathrm{PbL}^{4}\right]\left[\mathrm{N} \mathrm{O}_{3}\right]_{12}(\boldsymbol{\nabla}),\left[\mathrm{PbL}^{5}{ }_{2}\right](\mathbf{\Delta})$ and $\left[\mathrm{Pb}\left\{\mathrm{HB}(\mathrm{pz})_{3}\right\}_{2}\right]$ ( $\mathrm{pz}=$ pyrazolyl) (■), from refs. 23, 34, 32, 35-41 respectively. The $\mathrm{Pb}-\mathrm{L}$ distance decreases approximately as the donor atom $L$ is further from the proposed position of the lone pair

In more symmetric complexes such as $\left[M L^{1}\right]^{n+}\left(M^{n+}=\right.$ $\mathrm{Bi}^{3+}$ or $\mathrm{Pb}^{2+}$ ), the position of the lone pair is unambiguous, and it must lie along the four-fold axis through the square planes formed by the four nitrogen donors and the four oxygen donors. Its position is further indicated by the gap between the four oxygen donors, where it must be situated, and by the long $\mathrm{M}-\mathrm{O}$ bonds. The proposed positions of the lone pair in the more symmetric complexes of $\mathrm{Bi}^{11 \prime}$ and $\mathrm{Pb}^{\prime \prime}$ are indicated in Fig. 2. L awton and K okatailo ${ }^{33}$ have pointed out that in complexes of $P b^{\prime \prime}$ the lengths of the $M-L$ bonds decrease approximately as they are further away from the position of the lone pair. The distance of the donor atom from the lone pair on $\mathrm{Bi}^{\text {ilI }}$ or $\mathrm{Pb}^{\text {II }}$ can be quantified with the angle that the $\mathrm{M}-\mathrm{L}$ bonds form with the line passing through the centre of the postulated Ione pair and $\mathrm{Pb}^{\text {II }}$ or $\mathrm{Bi}^{\mathrm{II}}$. One can thus obtain (Fig. 3) a relationship between the $M-L$ distance and I.p. $-M-L$ angle (I.p. = lonepair), which shows bond lengthening with decreasing I.p. $-\mathrm{M}-\mathrm{L}$ angle. The further away a bond is from the lone pair, which is to say the larger the I.p. $-\mathrm{M}-\mathrm{L}$ angle, the shorter it is. The geometry around metal ions such as $\mathrm{Pb}^{11}$ and $\mathrm{Bi}^{11116}$ can be very irregular, as seen in Fig. 2, where the co-ordination geometry around $\mathrm{Pb}^{11}$ in its complex ${ }^{32}\left[\mathrm{PbL}^{2}(\mathrm{SCN})_{2}\right]$ is shown. The position of the lone pair, as proposed here, is also shown. For irregular complexes the lone pair can be located by examination of the bond lengths, and adjustment of the position of the lone pair to produce a relationship as shown in Fig. 3. Fig. 3 shows that this type of relationship holds quite well for complexes of Pb " and a variety of its complexes, ${ }^{30,32,34-40}$ and a similar relation is seen for some complexes ${ }^{11,16,23}$ of $\mathrm{Bi}^{11 \prime}$ in Fig. 4. The bond lengths to sulfur are corrected in Figs. 3 and 4 for the larger size of sulfur ${ }^{31}$ (with respect to nitrogen and oxygen) by subtraction of $0.3 \AA$, and for chloride are corrected by subtraction of $0.25 \AA$. The very long $\mathrm{Bi}-\mathrm{O}$ and $\mathrm{Pb}-\mathrm{O}$ bonds observed in structures such as that of the $L^{1}$ complexes ${ }^{12,30}$ can be seen to be the extreme case of extension of the $M-L$ bond when it is situated directly over the lone pair of electrons on the metal ion. The fairly large scatter of points in F igs. 3 and 4 may reflect steric effects, which are in addition to the effects of the lone pair on the $M-L$ bond length. Thus, one $\mathrm{Bi}-\mathrm{O}$ bond in the $[\mathrm{Bi}(\mathrm{Hedta})]$ complex, ${ }^{16}$ which is rather shorter than might have been anticipated from its closeness to the lone pair, may be short because it is part of a chelate ring, and its ability to move out to long $\mathrm{Bi}-\mathrm{O}$ lengths is limited sterically. On the other hand, oxygen atoms that form bridges between two metal ions appear to form $\mathrm{M}-\mathrm{O}$ bonds


Fig. 4 Relationship between $\mathrm{Bi}-\mathrm{L}$ length in some complexes of $\mathrm{Bi}^{\mathrm{II} \mathrm{\prime}}$, and I.p. $-\mathrm{Bi}-\mathrm{L}$ angle: $\left[\mathrm{Bi}(\right.$ cyclen $\left.)\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{ClO}_{4}\right)_{3}\right](\boldsymbol{\nabla})$, $\left[\mathrm{BiL}^{1}\right]\left[\mathrm{ClO}_{4}\right]_{3}$ ( $\square$ ), $\left[\mathrm{Bi}(\mathrm{nta})\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\right](\bigcirc),\left[\mathrm{Bi}(\mathrm{H}\right.$ edta) $](\mathrm{O}),[\mathrm{Bi}(\mathrm{dtpa})]^{2-}(\nabla)\left\{\mathrm{H}_{5} \mathrm{dtpa}=[(\mathrm{carb}-\right.$ oxymethyl) imino bbis(ethylenedinitrilo)tetraacetic acid\}, $\left[\left(\mathrm{BiL}^{4}\right)_{3}\right] \mathrm{Cl}_{9}$ (■). Structural data from this work, and refs. 12,16 and 39 . The Bi-L distance decreases approximately as the donor atom $L$ is further from the proposed position of the lone pair
that are longer than might be expected, which again might be due to steric effects preventing closer approach of the two complexes forming the dimer. One should point out that the structures used in drawing Figs. 3 and 4 were not selected for any particular reason, except that they were those which had already been extracted from the Cambridge Crystallographic D ata Base for other purposes.
The curves that have been drawn tentatively through the points in Figs. 3 and 4 suggest that $\mathrm{Bi}^{\prime \prime 1}$ and $\mathrm{Pb}^{\prime \prime}$ can be viewed as being ovoid, rather than effectively spherical as are pre-transition-metal ions of similar charge and size such as La'l' or Sr'I. An extensive analysis of the many structures available for complexes of $\mathrm{Pb}^{\prime \prime}$ is presently being carried out, with the hope that a molecular mechanics model can be developed where the strain-free $\mathrm{Pb}-\mathrm{L}$ bond length is a function of the angle made by the $\mathrm{Pb}-\mathrm{L}$ bond with the position of the Ione pair. It should al so be possible to develop a similar model for $\mathrm{Bi}^{\mathrm{II} \mathrm{\prime}}$, for which fewer structures are available.

The observation that $\mathrm{Pb}-\mathrm{L}$ or $\mathrm{Bi}-\mathrm{L}$ bonds become shorter as the I.p. $-\mathrm{M}-\mathrm{L}$ angle approaches $180^{\circ}$ suggests an analogy with the co-ordination geometry of $\mathrm{Hg} \mathrm{g}^{\prime \prime}$. The typical geometry for mercury(II) compounds is ${ }^{42}$ a distorted octahedron with two short bonds along one axis, which in the extreme case with highly covalent $\mathrm{Hg}-\mathrm{L}$ bonds such as in $\mathrm{Hg}(\mathrm{CN})_{2}$ becomes linear two-co-ordinate. This linear co-ordination may represent sp (or sd) hybridization of the $\mathrm{Hg}^{\prime \prime}$. In the V SEPR (valence shell electron pair repulsion) formalism ${ }^{22}$ the geometry of atoms having one lone pair on them (e.g. N in $\mathrm{NH}_{3}$ ) is derived from similar compounds of atoms where a co-ordinated atom is present instead of a lone pair (e.g. C in $\mathrm{CH}_{4}$ ). Ions such as $\mathrm{Pb}^{11}$ and Bi'l may be regarded as isoelectronic with $\mathrm{Hg} \mathrm{g}^{11}$ if the Ione pair of electrons on $\mathrm{Pb}^{1 \prime}$ and $\mathrm{Bi}^{11 \prime}$ is considered to be a pair of electrons donated by a donor atom, as required by the VSEPR formalism. Thus, $\mathrm{Pb}^{\text {"I }}$ and $\mathrm{Bi}^{\mathrm{I} \mathrm{\prime} \mathrm{\prime}}$ would have a preference for a linear co-ordination geometry similar to that of $\mathrm{Hg}^{11}$, with the lone pair on $\mathrm{Pb}^{\prime \prime}$ and $\mathrm{Bi}^{\prime \prime \prime}$ occupying one of the two coordination sites found in linearly co-ordinated $\mathrm{Hg}^{\prime \prime}$, in line with V SE PR ideas. ${ }^{22}$ This suggestion is illustrated in Fig. 5. The analogy accounts for the fact that bonds at right angles to the lone pair on $\mathrm{Pb}^{\prime \prime}$ and $\mathrm{Bi}^{\mathrm{I} \mathrm{\prime} \mathrm{\prime}}$ are longer than those opposite the Ione pair. The preference ${ }^{1-5}$ of $\mathrm{Hg}^{11}$ for linear co-ordination geometry is also reflected in the formation constants of its complexes. Complexes of ligands where two donor atoms can occupy the two co-ordination sites $180^{\circ}$ apart are more stable than those where they cannot. Thus, for $\mathrm{Hg}^{11}, \log \mathrm{~K}_{1}$ for the ethane-1,2-diamine (en) complex is ${ }^{17}$ much lower than that


Fig. 5 The VSEPR ${ }^{22}$ analogy proposed here between the preferred linear two-co-ordination found in complexes of Hg gi above, and the 'one-co-ordinate' geometry towards which $\mathrm{Pb}^{\prime \prime}$ (and $\mathrm{Bi}^{\prime \prime \prime}$ ) tends, although a definite one-co-ordinate structure of $\mathrm{Pb}^{\text {II }}$ (or of $\mathrm{Bi}^{\text {III }}$ ) has not so far been observed. This proposal accounts for the fact that Pb-L and $\mathrm{Bi}-\mathrm{L}$ bonds are shortest when directly opposite the lone pair, which is held to occupy one of the two co-ordination sites found on linearly co-ordinated H g'
with $L^{6}$, presumably because the long connecting bridge of the latter allows the two nitrogens to co-ordinate $180^{\circ}$ apart on the $\mathrm{Hg}^{\mathbf{\prime \prime}}$, while for en the bridge is too short. For $\mathrm{Pb}^{\mathbf{\prime \prime}}$, high stability would be expected for unidentate ligands which would occupy only the site opposite the lone pair, and as the donor atoms were forced to be further apart, and hence closer to the lone pair, so complex stability would diminish. Thus, it has been found ${ }^{43}$ that tertiary monoamines such as triethylamine form complexes of unprecedented stability with $\mathrm{Pb}^{\prime \prime}$, with a $\log \mathrm{K}_{1}$ value of about 5.3 , which can be contrasted with $\log K_{1}$ with en ${ }^{17}$ of only 5.04 . It is presumed that in the triethylamine complexes the unidentate amine occupies a position $180^{\circ}$ from the lone pair, with a short $\mathrm{Pb}-\mathrm{N}$ bond, which Fig. 3 suggests may be between 2.2 and $2.3 \AA$ in length. The Pb"I may be effectively one-co-ordinate in such a complex, with only long bonds to coordinated solvent molecules, or counter ions, similar to thelong bonds at right angles to the sp hybrid orbitals in mercury(iI) complexes.

A further problem to be dealt with is that of complexes where there does not appear to be a stereochemically active lone pair on $\mathrm{Bi}^{11 \prime}$ or $\mathrm{Pb}^{\prime \prime}$, such as the lead(ir) complex with cryptand 222 (4,7,13,16,21,24-hexaoxa-1,10-diazabicyclo[8.8.8]hexacosane), ${ }^{44}$ the tris-terpy complex ${ }^{45}$ (terpy $=2,2^{\prime}: 6^{\prime}, 2^{\prime \prime}$-terpyridine) and the bis-tren complex ${ }^{46}$ [tren $\left.=\operatorname{tris}(2-a m i n o e t h y l) a m i n e\right]$. The cause of the non-stereochemically active lone pair may be electronic, or it can also be steric, as has been shown ${ }^{41}$ for complexes of $\mathrm{Pb}^{\prime \prime}$ with methyl-substituted tris(pyrazolyl)borate. It has been pointed out ${ }^{47}$ that in complexes of $\mathrm{Pb}^{11}$ and $\mathrm{Sn}^{11}$ where the structure suggests that the lone pair is not stereochemically active, the metal atom has very large thermal parameters. This is not true for the above complexes of $\mathrm{Pb}^{\mathbf{1 1}}$ where the lone pair is

Table 4 Formation constant for $\mathrm{Bi}^{\text {III }}$ with cyclen determined polarographically, together with protonation constants of cyclen and hydrolysis constants of $\mathrm{Bi}^{1 \mathrm{II}}$ used to calculate $\log \mathrm{K}_{\mathbf{1}}$. Ionic strength 0.5 $\mathrm{mol} \mathrm{dm}{ }^{-3}, 25^{\circ} \mathrm{C}$

| Equilibrium | $\log K$ | R ef. |
| :---: | :---: | :---: |
| $\mathrm{H}^{+}+\mathrm{OH}^{-} \rightleftharpoons \mathrm{H}_{2} \mathrm{O}$ | 13.74 | 17 |
| $\mathrm{H}^{+}+\mathrm{L} \rightleftharpoons \mathrm{HL}^{+}$ | 10.82 | 17 |
| $\mathrm{H}^{+}+\mathrm{HL}^{+} \rightleftharpoons \mathrm{H}_{2} \mathrm{~L}^{2+}$ | 9.72 | 17 |
| $\mathrm{H}_{2} \mathrm{~L}^{2+}+\mathrm{H}^{+} \rightleftharpoons \mathrm{H}_{3} \mathrm{~L}^{3+}$ | 1.15 | 17 |
| $\mathrm{Bi}^{3+}+\mathrm{L} \rightleftharpoons[\mathrm{BiL}]^{3+}$ | $23.45 \pm 0.05$ | This work |
| $\mathrm{Bi}^{3+}+\mathrm{OH}^{-} \rightleftharpoons[\mathrm{Bi}(\mathrm{OH})]^{2+}$ | 12.42 | 17 |
| $\mathrm{Bi}^{3+}+3 \mathrm{OH}^{-} \rightleftharpoons \mathrm{Bi}(\mathrm{OH})_{3}$ | 31.88 | 17 |
| $\mathrm{Bi}^{3+}+4 \mathrm{OH}^{-} \rightleftharpoons\left[\mathrm{Bi}(\mathrm{OH})_{4}\right]^{-}$ | 32.98 | 17 |
| $6 \mathrm{Bi}^{3+}+12 \mathrm{H}^{-} \rightleftharpoons\left[\mathrm{Bi}_{6}(\mathrm{OH})_{12}\right]^{6+}$ | 162.78 | 17 |
| $9 \mathrm{Bi}^{3+}+200 \mathrm{H}^{-} \rightleftharpoons\left[\mathrm{Bi}_{9}(\mathrm{OH})_{20}\right]^{7+}$ | 266.92 | 17 |
| $9 \mathrm{Bi}^{3+}+210 \mathrm{H}^{-} \rightleftharpoons\left[\mathrm{Bi}_{9}(\mathrm{OH})_{21}\right]^{6+}$ | 276.76 | 17 |
| $9 \mathrm{Bi}^{3+}+22 \mathrm{OH}{ }^{-} \rightleftharpoons\left[\mathrm{Bi}_{9}(\mathrm{OH})_{22}\right]^{5+}$ | 287.30 | 17 |

not stereochemically active. It may be that in some complexes where the lone pair does not appear to be stereochemically active there is dynamic disorder between two identical structures each with a stereochemically active lone pair, which gives an overall apparently higher symmetry to the complex, and an appearance of there being no stereochemically active lone pair.

## Complex formation of $\mathrm{Bi}^{\text {III }}$ with cyclen

In Fig. 6 are shown selected DP polarograms for the Bill_ cyclen system at various pH values, after 7 months of equilibration. These polarograms show typical non-labile behaviour. With increase of pH the height of the $\mathrm{Bi}^{3+}$ peak decreases, and a well separated peak for the Bi'II-cyclen complex appears at a value some 400 mV more negative. The peak referred to as the $\mathrm{Bi}^{3+}$ peak in fact corresponds ${ }^{10}$ to a mixture of $\mathrm{Bi}^{3+}$ and hydrolysed species, the composition of which varies with pH , so that its height cannot be used in a simple direct way to calculate the concentration of uncomplexed $\mathrm{Bi}^{3+}$. It represents a labile mixture of $\left[\mathrm{Bi}_{\mathrm{m}}(\mathrm{OH})_{n}\right]^{(3 \mathrm{~m}-\mathrm{n})+}$ species, so that the concentration of free $\mathrm{Bi}^{3+}$ has to be calculated by solving the appropriate mass-balance equation (4) where $[M]_{T(l a b)}$ is the total metal-ion

$$
\begin{equation*}
[M]_{T(\text { lab })}=[M]_{\text {free }}+\sum_{j=1}^{m} \sum_{i=1}^{n} j \beta_{i j}[M]_{\text {free }}[O H]^{i} \tag{4}
\end{equation*}
$$

concentration excluding that bound up as the non-labile ML complex, $[M]_{\text {free }}$ is the free metal-ion concentration, and $\beta_{\mathrm{ij}}$ is the formation constant of the hydrolysed species $\mathrm{Bi}_{\mathrm{j}}(\mathrm{OH})_{\mathrm{i}}$. The free metal-ion concentration is thus calculated with M L SPEC ${ }^{\mathbf{3 0}}$ and the known ${ }^{17}$ formation constants of the $M_{j}(O H)_{i}$ species, from the height of the ' $\mathrm{Bi}^{3+\prime}$ peak. The free pro-ligand concentration was calculated from the appropriate mass-balance equation and the protonation constants ${ }^{17}$ of cyclen at ionic strength $0.5 \mathrm{~mol} \mathrm{dm}{ }^{-3}$. The concentration of the $\mathrm{Bi}^{\text {III }}$-cyclen complex was calculated from the sum of the bismuth(iII) species ( $\mathrm{B}^{\mathrm{i}^{3+}}$ plus hydrolysed species) not complexed by cyclen. The set of $\mathrm{Bi}^{\text {III }}$-cyclen solutions gave calculated values of $\log \mathrm{K}_{1}$ of 23.17, 23.37, 23.45 and 23.45 after 1, 3, 6 and 7 months had elapsed. Table 4 shows the formation constant determined for Bilit with cyclen, together with the constants for formation of hydrolysed bismuth(iII) species used in the calculation of $\log K_{1}$.

The Bi'II-cyclen complex is of high stability, as was found ${ }^{10,11}$ for the bismuth(III) complexes of [14]aneN 4 and [15]aneN ${ }_{4}$. The pattern that is emerging with the bismuth(III) complexes of the tetraazamacrocycles is that the variation of the formation constants with macrocyclic ring size resembles that of $C d^{\prime \prime}$, which is similar in size ${ }^{31}$ to $\mathrm{Bi}^{\text {III }}$ (Table 5).

Extensive work has shown ${ }^{48,49}$ that the metal-ion selectivity of the tetraazamacrocycles is more complex than envisaged in the simple 'size match selectivity' concept. If the complexes are allowed to adopt whichever ligand conformation and metal-

Table 5 Formation constants of tetraazamacrocyclic ligands with a selection of metal ions

| M etal ion | $\mathrm{r}^{+} / \AA$ | $\log K_{1}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $[12] \mathrm{aneN}_{4}$ <br> (cyclen) | [13]aneN 4 | [14]aneN 4 (cyclam) | [15]aneN 4 | [16]aneN 4 |
| Cu'l | 0.57 | 23.4 | 24.4 | 27.2 | 24.4 | 21.6 |
| $\mathrm{Zn}{ }^{\prime \prime}$ | 0.74 | 16.2 | 15.6 | 15.5 | 15.0 | 13.1 |
| $C d^{\prime \prime}$ | 0.95 | 14.3 | 12.7 | 11.2 | 12.1 | 12.7 |
| Bi'I' | 1.03 | 23.45 | - | 21.5 | 23.5 | - |
| Pb' | 1.18 | 15.9 | 13.5 | 10.8 | 10.2 | 9.6 |

Formation constants from refs. 10, 11, 17 and this work. Ionic radii ( $r^{+}$) from ref. 31. [13]ane $N_{4}=1,4,7,11$-Tetraazacyclotridecane.


Fig. 6 A selection of polarograms at different pH values recorded for Bili-cyclen solutions after equilibration for 7 months. The total Bill' was initially, before addition of base to raise the $\mathrm{pH}, 2.44 \times 10^{-4} \mathrm{~mol}$ $\mathrm{dm}^{-3}$ and the $\mathrm{L}: \mathrm{M}$ ratio 50.8:1
ion geometry that is of lowest strain energy, then in fact ${ }^{49}$ the cavities of the tetraazamacrocycles decrease from [12]aneN 4 (square pyramidal) through [14]aneN $\mathrm{N}_{4}$ (square planar) to [16]ane $\mathrm{N}_{4}$ (tetrahedral). The upturn in complex stability from [14]aneN 4 to [15]aneN 4 found only for $\mathrm{Bi}^{\text {III }}$ and the similarly sized $C d^{11}$ must relate to some unusual feature of the coordination in these complexes.

This study has attempted to analyse the structure and stability of complexes of Bi'I, and also of Pb". The complex effects of the lone pair of electrons on these metal ions may be understood through the analogy presented here, where the lone pair occupies one co-ordination site in linear two-co-ordinate geometry like that of $\mathrm{Hg}^{\prime \prime}$, that tends towards, but so far has not been observed to achieve, a one-co-ordinate status in $\mathrm{Bi}^{\text {III }}$ and $P b^{\prime \prime}$. The $\mathrm{M}-\mathrm{L}$ bonds in $\mathrm{Bi}^{\text {III }}$ and $\mathrm{Pb}^{\text {II }}$ thus lengthen as they move further away from the preferred site of co-ordination opposite the lone pair. The lone pair can be located more accurately by an analysis where its position is related to the extent of lengthening of the $M-L$ bonds observed. There does therefore not have to be an obvious gap in the co-ordination geometry on $\mathrm{Pb}^{I \prime}$ and $\mathrm{Bi}^{\mathrm{II} \mathrm{\prime} \mathrm{\prime}}$ to locate the lone pair. The presence of the latter can be indicated simply by the pattern of long and short bonds to the metal ion. The previous suggestion ${ }^{23}$ that the lone pair in the $L^{1}$ and the $L^{2}$ complexes of $P b^{11}$ was not stereochemically active should therefore be revised. A n important question is the nature of the attraction that occurs for donor atoms which lie directly over the lone pair, with very long contacts of about $3.5 \AA$. A lthough M OPAC ${ }^{50}$ does not perform particularly well in our experience in calculations aimed at predicting the structures of complexes of $\mathrm{Pb}^{\prime \prime}$ or $\mathrm{Bi}^{\prime \prime \prime}$, the calculations we have so far carried out, and which will be reported in a future paper together with more ambitious ab initio calculations, give an indication of the nature of these very long contacts. In com-
pounds of more electronegative atoms such as nitrogen, wavemechanical calculations at all levels of complexity show regions of significant negative charge at the position of the lone pair. In M OPAC calculations on $\mathrm{BiL}_{3}$ complexes, however, there is no negative charge at the position of the lone pair, but rather a region where the positive charge is lower than on the rest of the Bi atom. There is thus still a positive charge, although it is closer to neutral, in the region of the lone pair on $\mathrm{Bi}^{\mathrm{III}}$, and it is this which would produce the weak interactions with donor atoms in the vicinity of the lone pair, resulting in the long contacts observed in some structures.

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